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Tempo and Beat Analysis



Introduction

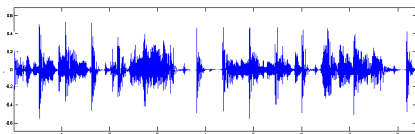
Musical Properties:

- Harmony
- Melody
- Rhythm
- Timbre

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Introduction

Perception of Rhythm:



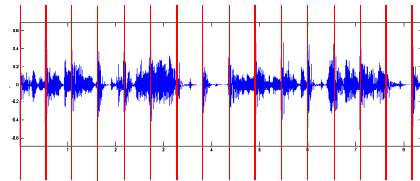
1. Musical accents → Beats
2. Regular intervals, periodicity → Tempo

Tapping your Foot

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Introduction

Perception of Rhythm:



1. Musical accents → Beats
2. Regular intervals, periodicity → Tempo

Tapping your Foot

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Examples: Strong or weak rhythm?

- Queen – Another One Bites The Dust ▶
- Shostakovich – 2nd Waltz ▶
- Beethoven – Pathétique ▶
- Beethoven – Symphony No. 5 ▶
- Borodin – String Quartet No. 2 ▶

Musical Timings

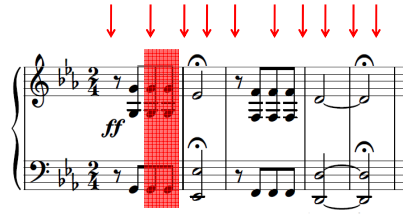
Musical tempo may differ from perceived tempo!



Musical Timings

Tempo and beat analysis on different time scales:

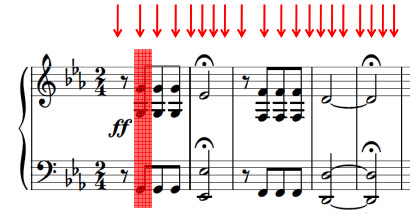
Tactus (beat) Level



Musical Timings

Tempo and beat analysis on different time scales:

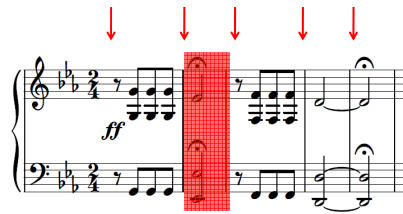
Tatum (*temporal atom*) Level



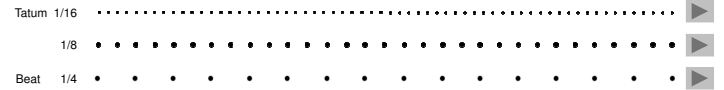
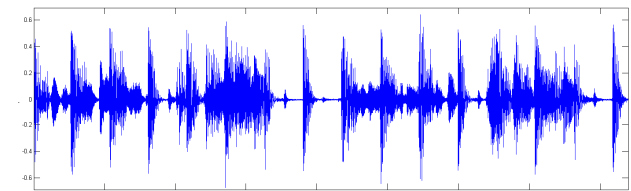
Musical Timings

Tempo and beat analysis on different time scales:

Measure Level



Beat



Beat Tracking

1. Impulse Extraction
2. Periodicity Analysis

3. Musical Tempo Estimation
4. Tracking *the* Beat



Beat Tracking

1. Impulse Extraction **Signal Processing**
2. Periodicity Analysis

3. Musical Tempo Estimation **Musical Knowledge**
4. Tracking *the* Beat



Impulse Extraction

- Musical Accents

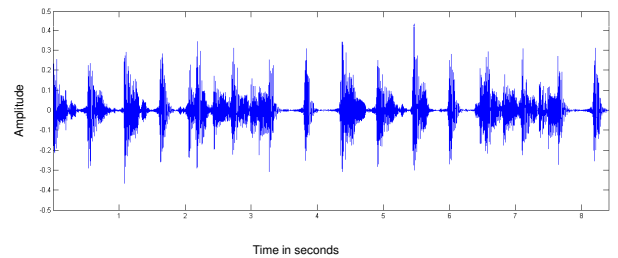
Onsets:

- The exact time, a note is hit
- One of the three parameters defining a note (pitch, onset, duration)
- Change of perceived properties of sound:
 - Loudness
 - Pitch
 - Timbre



Impulse Extraction

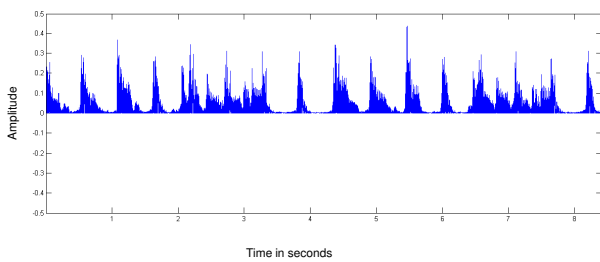
- Rectification
- Smoothing
- Differentiation
- Half wave rectification



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Impulse Extraction

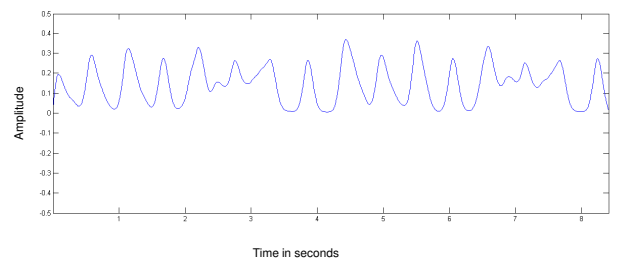
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Impulse Extraction

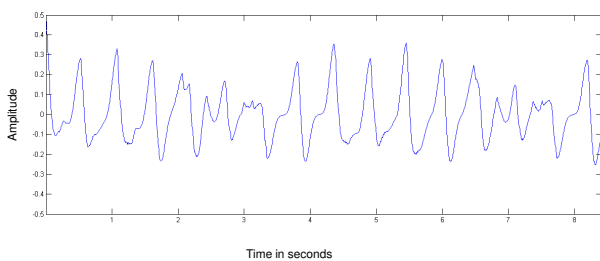
- Rectification
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Impulse Extraction

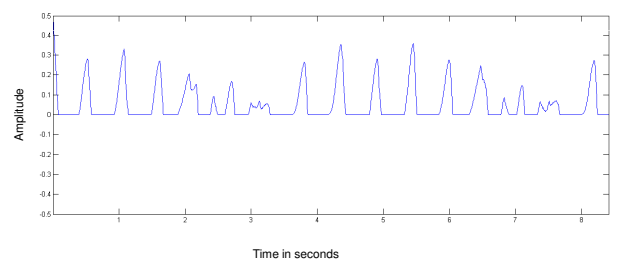
- Rectification
- Smoothing
- Differentiation
- Half wave rectification



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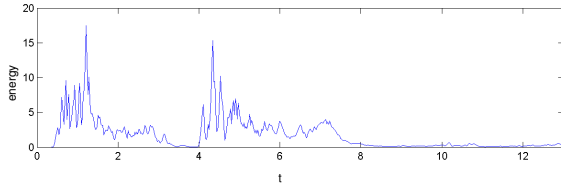
Impulse Extraction

- Rectification
- Smoothing
- Differentiation
- Half wave rectification

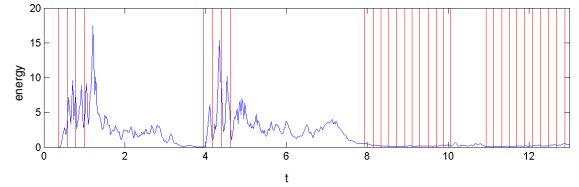


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Classical Music

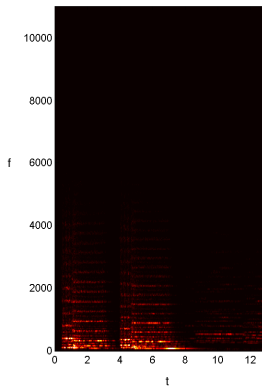


Classical Music



Extraction of Transients

spectrogram $|X|$



1. Spectrogram
2. Log compression
3. Differentiation
4. Integration

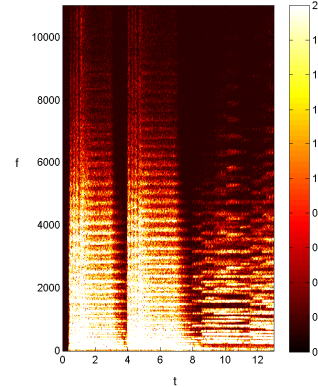
capture spectral changes:

- loudness
- pitch
- timbre

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Extraction of Transients

Compressed spectrogram Y



1. Spectrogram
2. Log compression
3. Differentiation
4. Integration

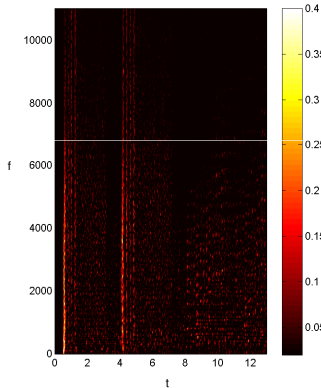
$$Y = \log(1 + C \cdot |X|)$$

- human sensation
- enhances low intensity values
- high frequency content
- reduces influence of amplitude modulation

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Extraction of Transients

Spectral difference



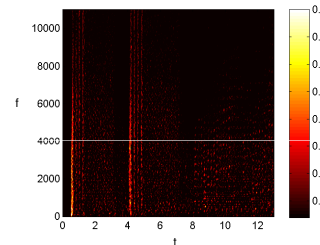
1. Spectrogram
2. Log compression
3. Differentiation
4. Integration

- measure of change
- only positive intensity changes
- relative difference function

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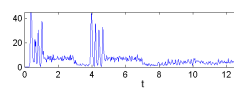
Extraction of Transients

Spectral difference



1. Spectrogram
2. Log compression
3. Differentiation
4. Integration

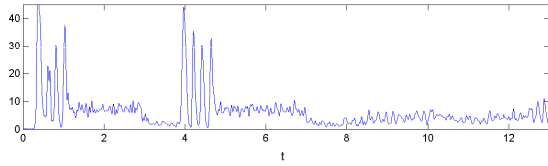
Novelty Curve



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Postprocessing

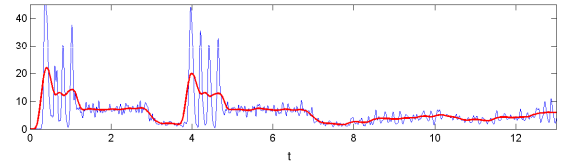
Novelty Curve



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Postprocessing

Novelty Curve

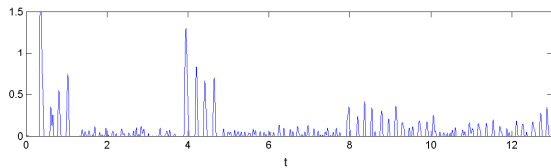


Subtraction of Local Average

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Novelty Curve

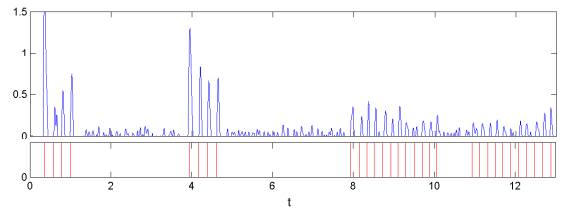
Novelty Curve



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Novelty Curve

Novelty Curve

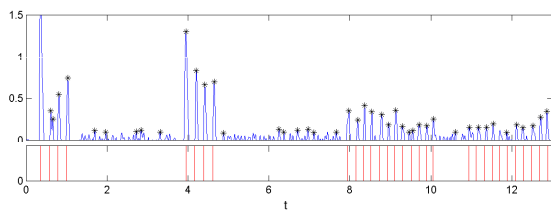


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Peak Picking

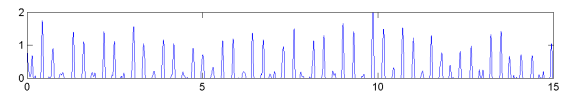
Peaks as note onset candidates: ▶

Novelty Curve

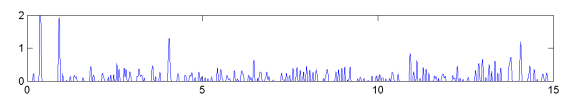


Examples

Shostakovich – 2nd Waltz ▶

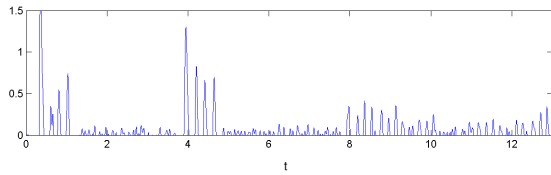


Borodin – String Quartet No. 2 ▶



Periodicity Estimation

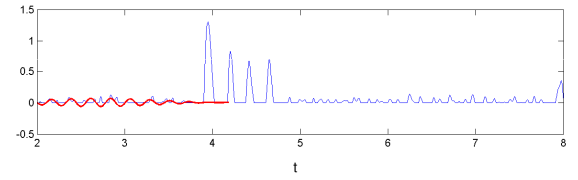
Reveal periodic structure of novelty curve
Frequency / Tempo



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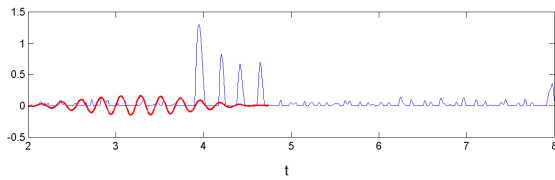
Fourier Analysis

Sinusoidal kernels
30 to 600 BPM, 0.5 to 10 Hz



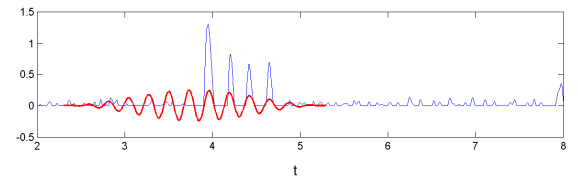
Fourier Analysis

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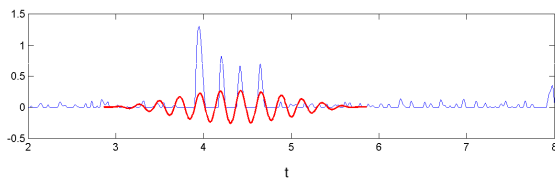
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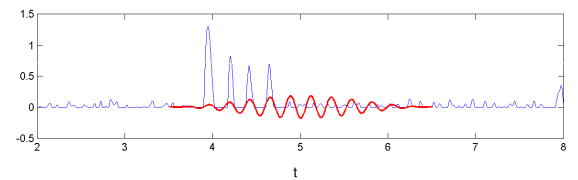
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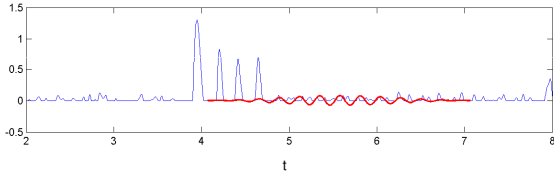
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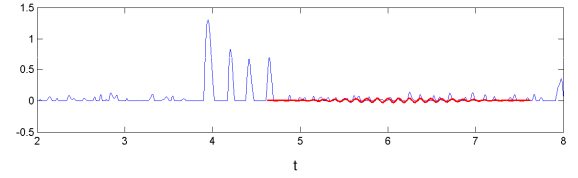
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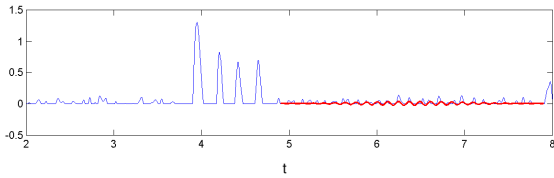
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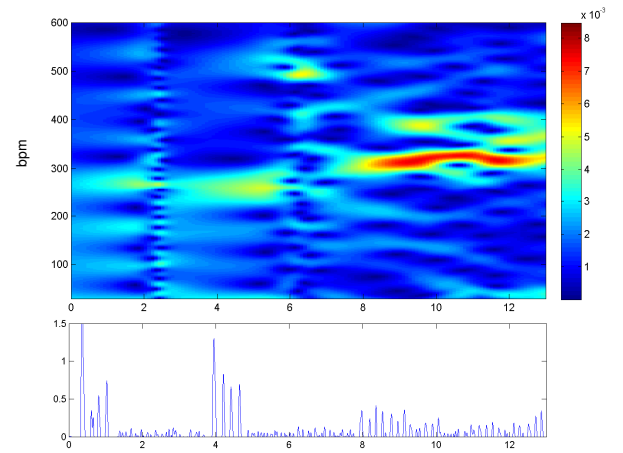


Fourier Analysis

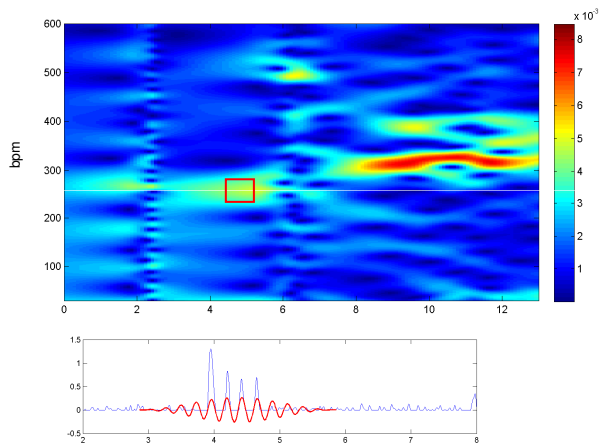
Sinusoidal kernels
30 to 600 BPM, 0.5 to 10 Hz



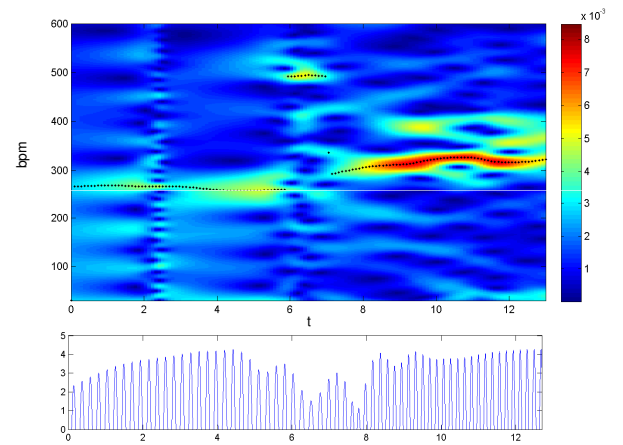
Tempogram



Tempogram



Tempogram: Optimal Periodicity Kernels



Examples:

- Queen – Another One Bites The Dust ▶
- Shostakovich – 2nd Waltz ▶

- Beethoven – Symphony No. 5 ▶
- Borodin – String Quartet No. 2 ▶

Summary

1. Impulse Extraction
 - Novelty curve (something is changing, note onsets)
 - Indicates note onset candidates
 - Hard task for non-percussive instruments (strings)
2. Periodicity Analysis
 - Fourier analysis
 - Detect ***a*** tempo (the dominant)
3. Musical Tempo Estimation
 - Define ***the*** tempo (quarter beats per minute)
 - Musical knowledge needed (meter, time signature, ...)
4. Tracking ***the*** Beat
 - Find most likely beat positions