



Eurographics 2012

Cagliari, Italy

May 13 -18

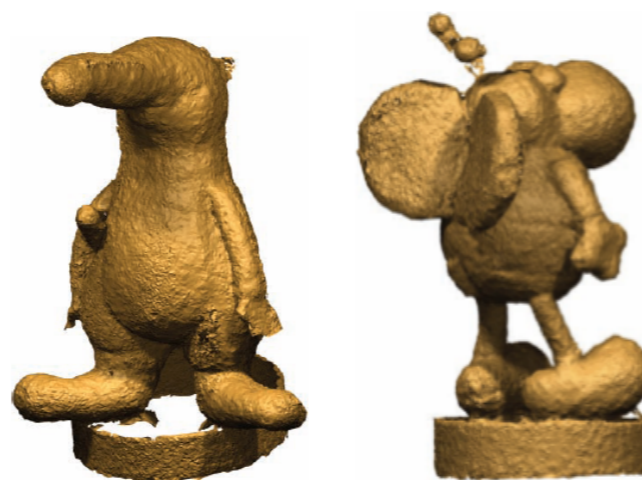


33rd ANNUAL CONFERENCE OF THE EUROPEAN ASSOCIATION FOR COMPUTER GRAPHICS

Dynamic Geometry Processing

EG 2012 Tutorial

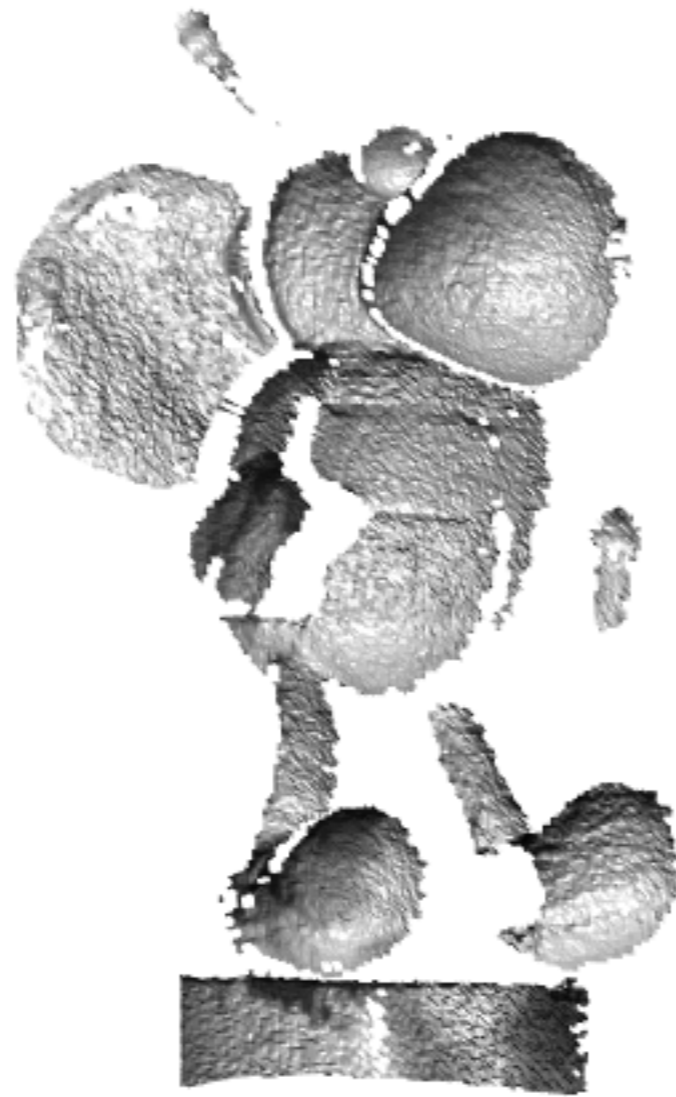
Dynamic Registration



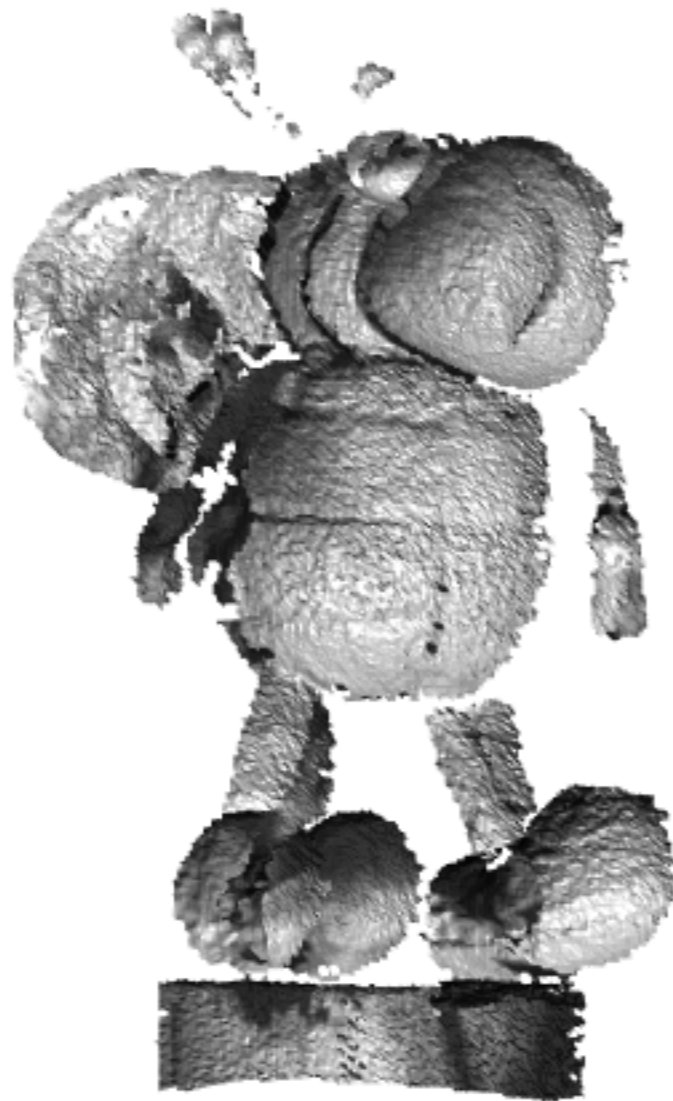
Niloy J. Mitra

University College London

Scan Registration



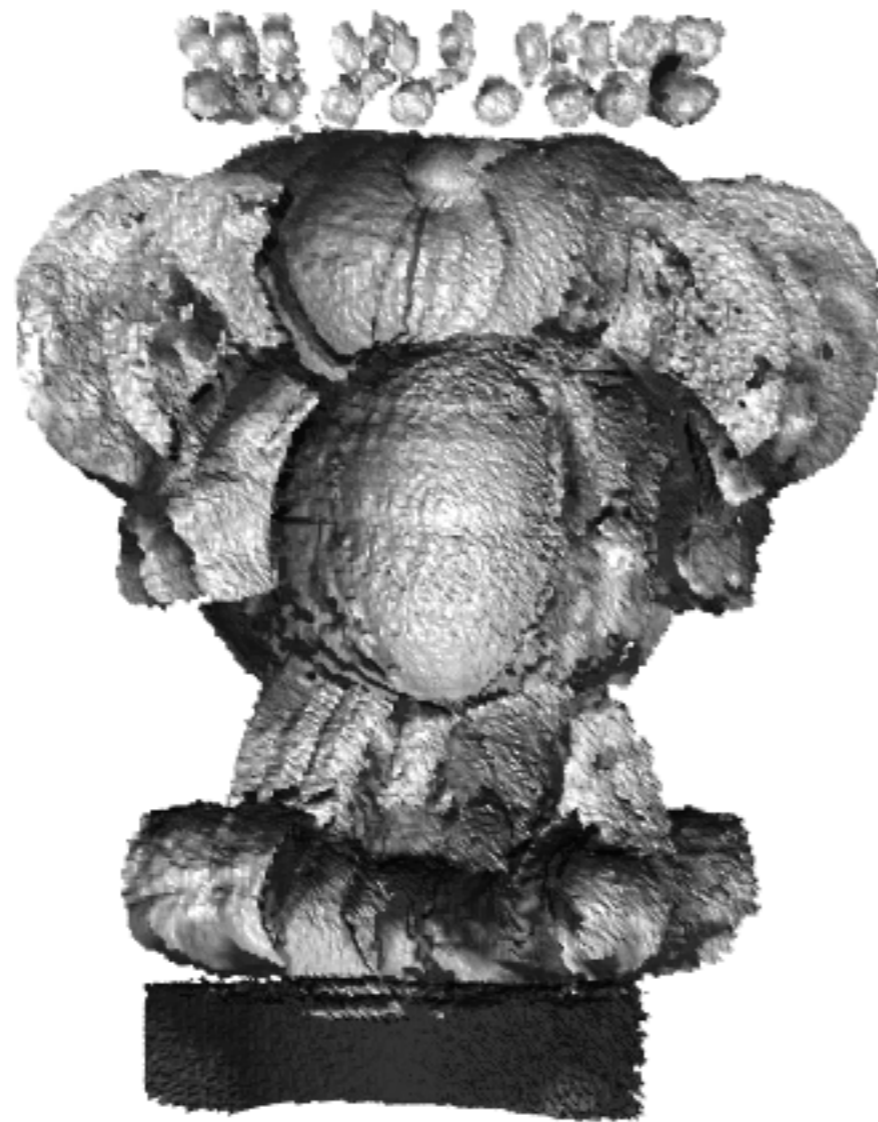
Scan Registration



Solve for inter-frame motion:

$$\alpha := (\mathbf{R}, \mathbf{t})$$

Scan Registration



Solve for inter-frame motion:

$$\alpha_j := (\mathbf{R}_j, \mathbf{t}_j)$$

The Setup

Given:

A set of frames $\{P_0, P_1, \dots, P_n\}$

Goal:

Recover rigid motion $\{\alpha_1, \alpha_2, \dots, \alpha_n\}$ between adjacent frames

The Setup

Smoothly varying object motion

Unknown correspondence between scans

Fast acquisition →

motion happens between frames

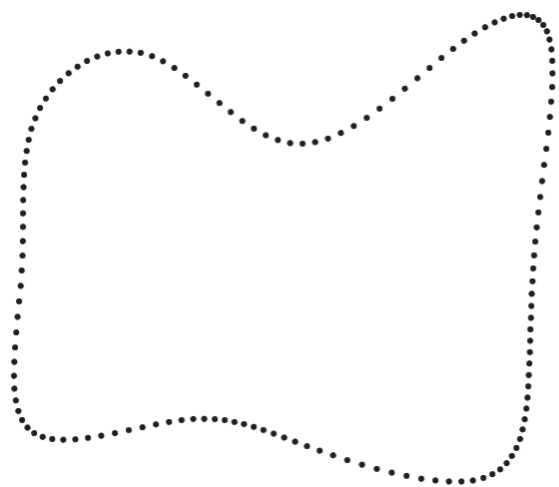
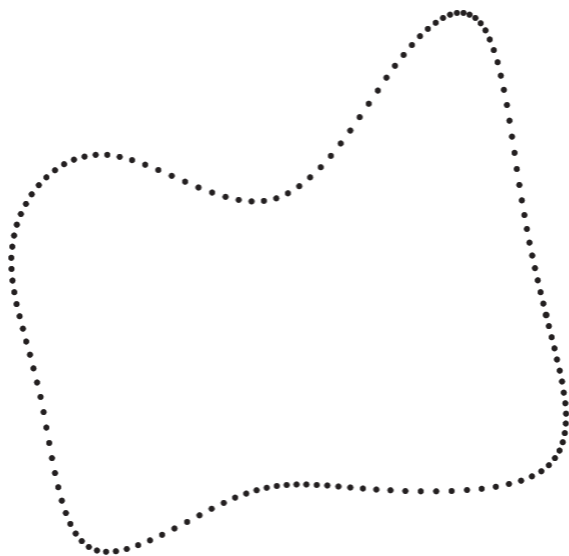
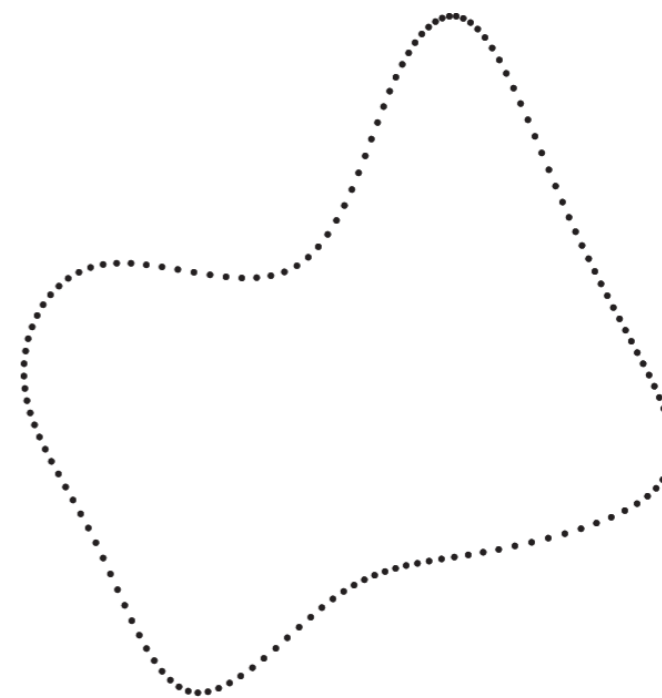
Insights

Rigid registration \rightarrow kinematic property of space-time surface (locally exact)

Registration \rightarrow surface normal estimation

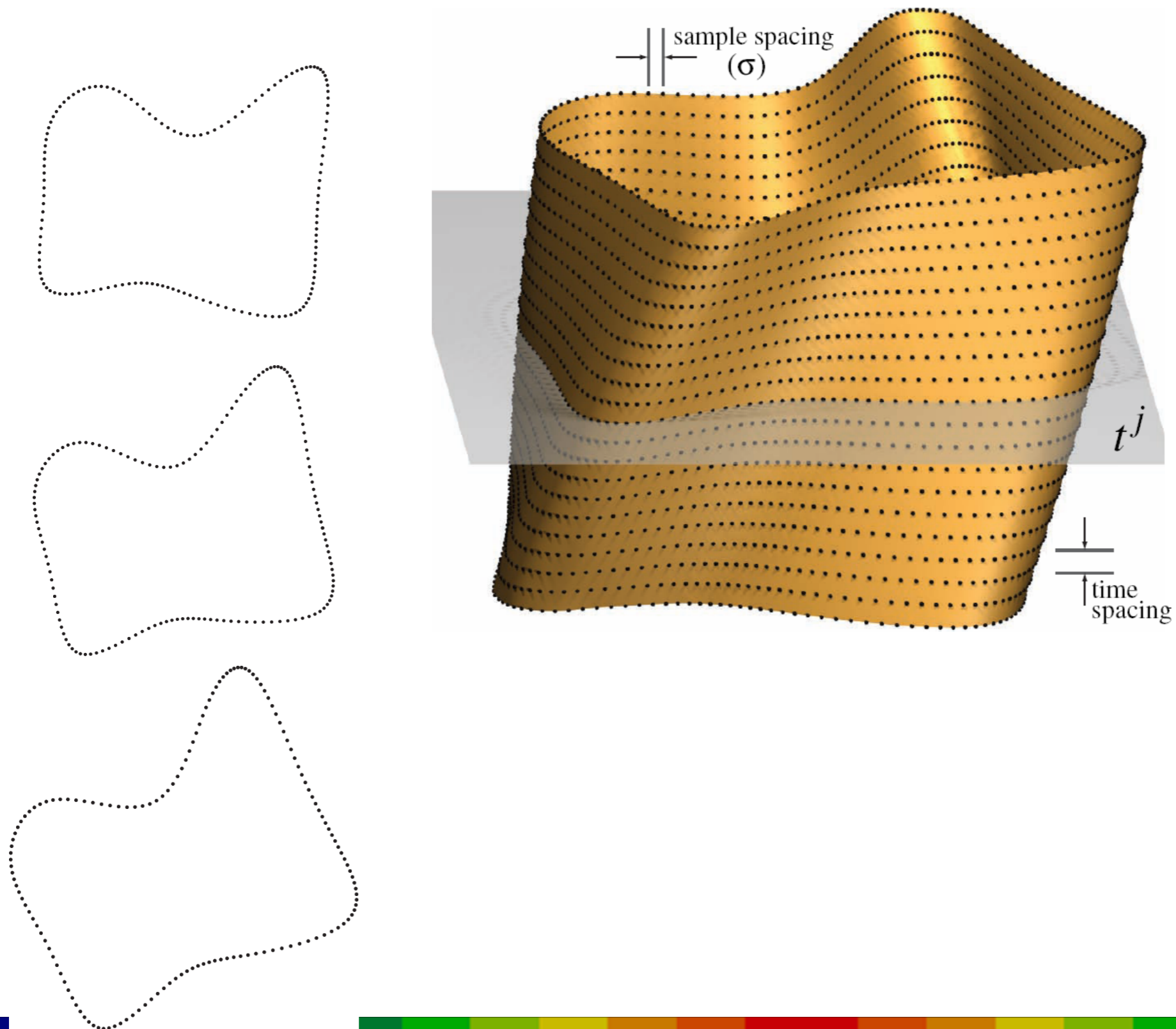
Extension to deformable/articulated bodies

Time Ordered Scans

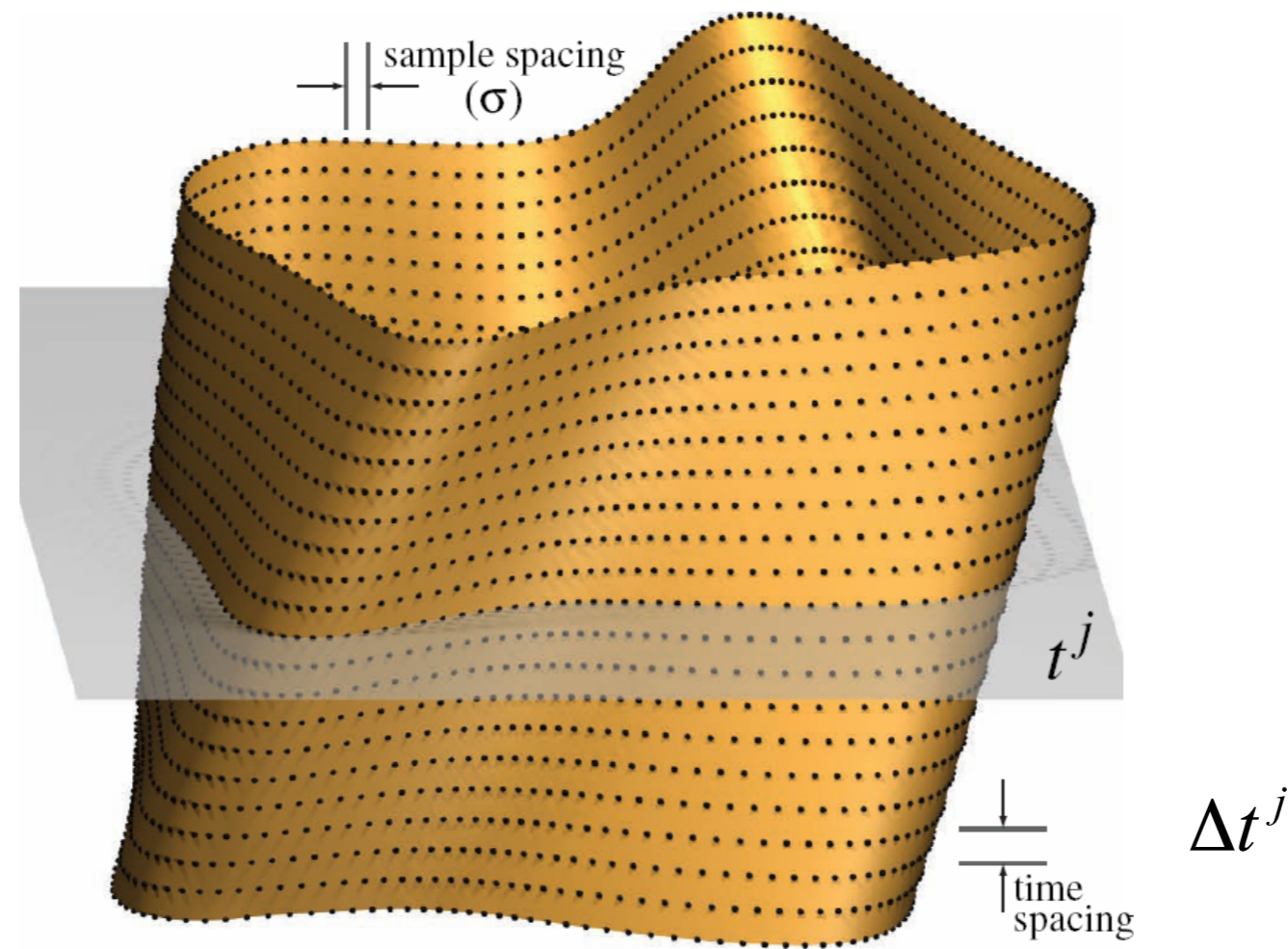
 t^j  t^{j+1}  t^{j+2}

$$\tilde{P}^j \equiv \{\tilde{\mathbf{p}}_i^j\} := \{(\mathbf{p}_i^j, t^j), \mathbf{p}_i^j \in \mathbb{R}^d, t^j \in \mathbb{R}\}$$

Space-time Surface

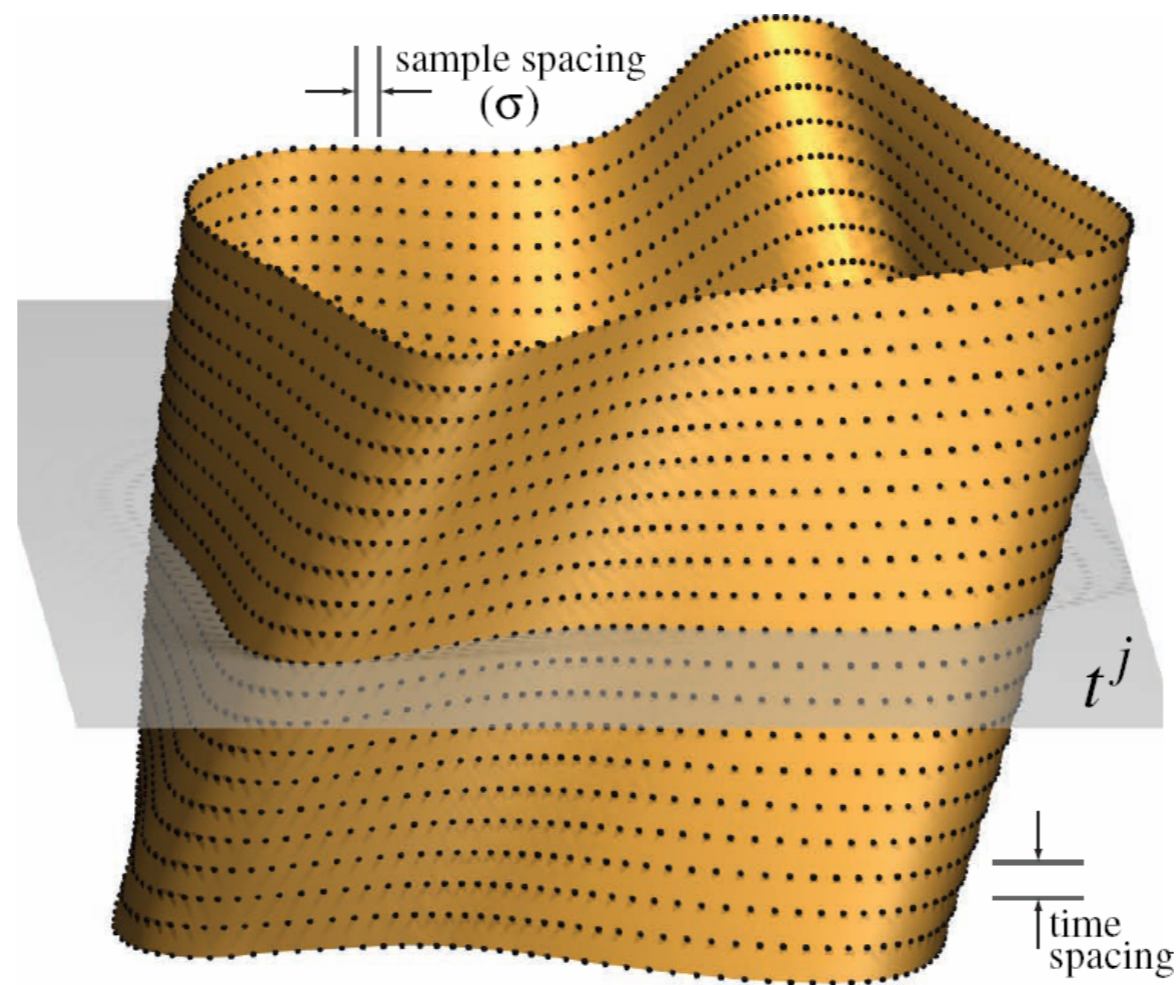


Space-time Surface



$$\tilde{\mathbf{p}}_i^j \quad \rightarrow \quad \tilde{\alpha}_j(\tilde{\mathbf{p}}_i^j) = \left(\mathbf{R}_j \mathbf{p}_i^j + \mathbf{t}_j, \boxed{t^j + \Delta t^j} \right)$$

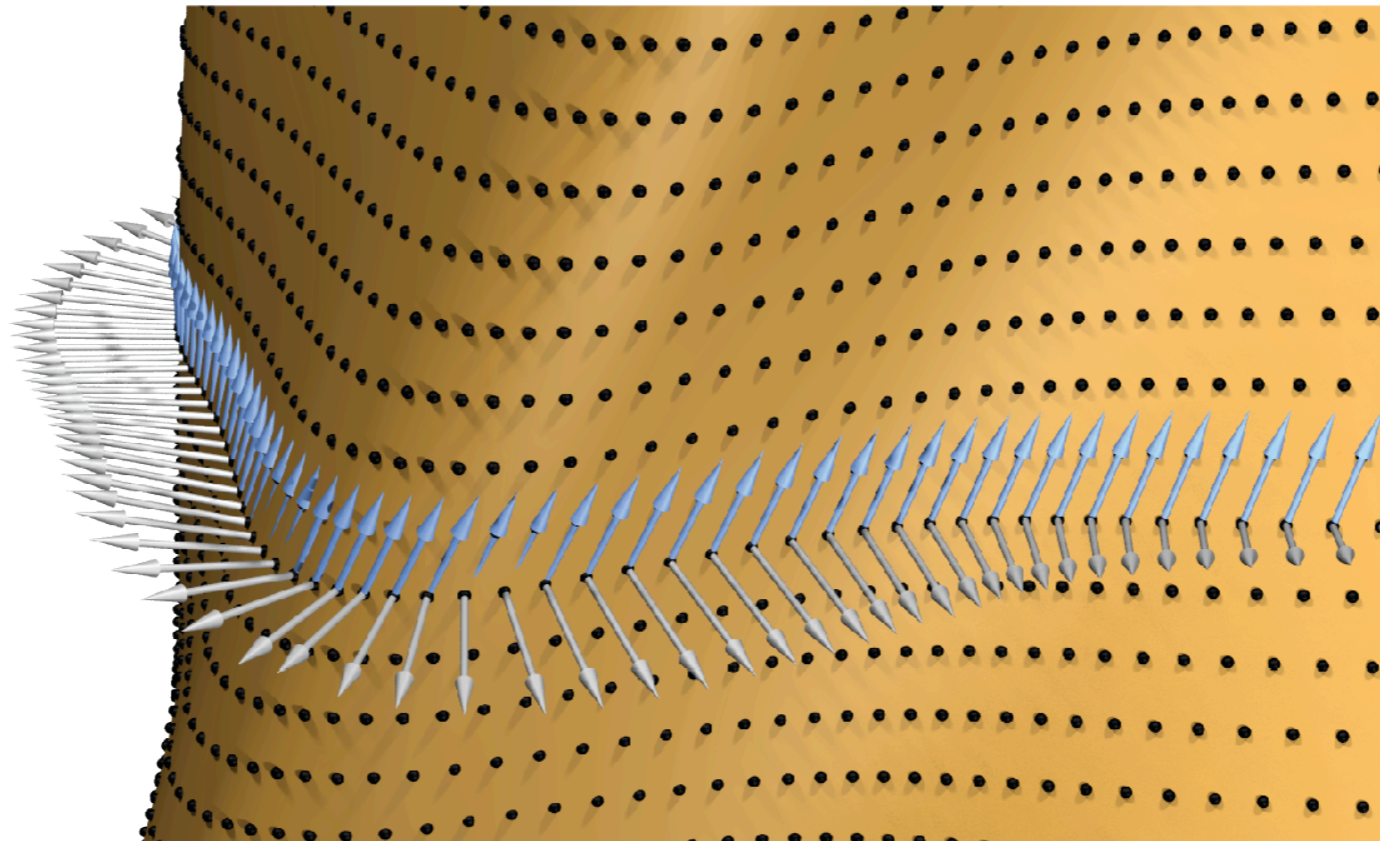
Space-time Surface



$$\tilde{\mathbf{p}}_i^j \rightarrow \tilde{\alpha}_j(\tilde{\mathbf{p}}_i^j) = \left(\mathbf{R}_j \mathbf{p}_i^j + \mathbf{t}_j, t^j + \Delta t^j \right)$$

$$\tilde{\alpha}_j = \operatorname{argmin} \sum_{i=1}^{|P^j|} d^2(\tilde{\alpha}_j(\tilde{\mathbf{p}}_i^j), S)$$

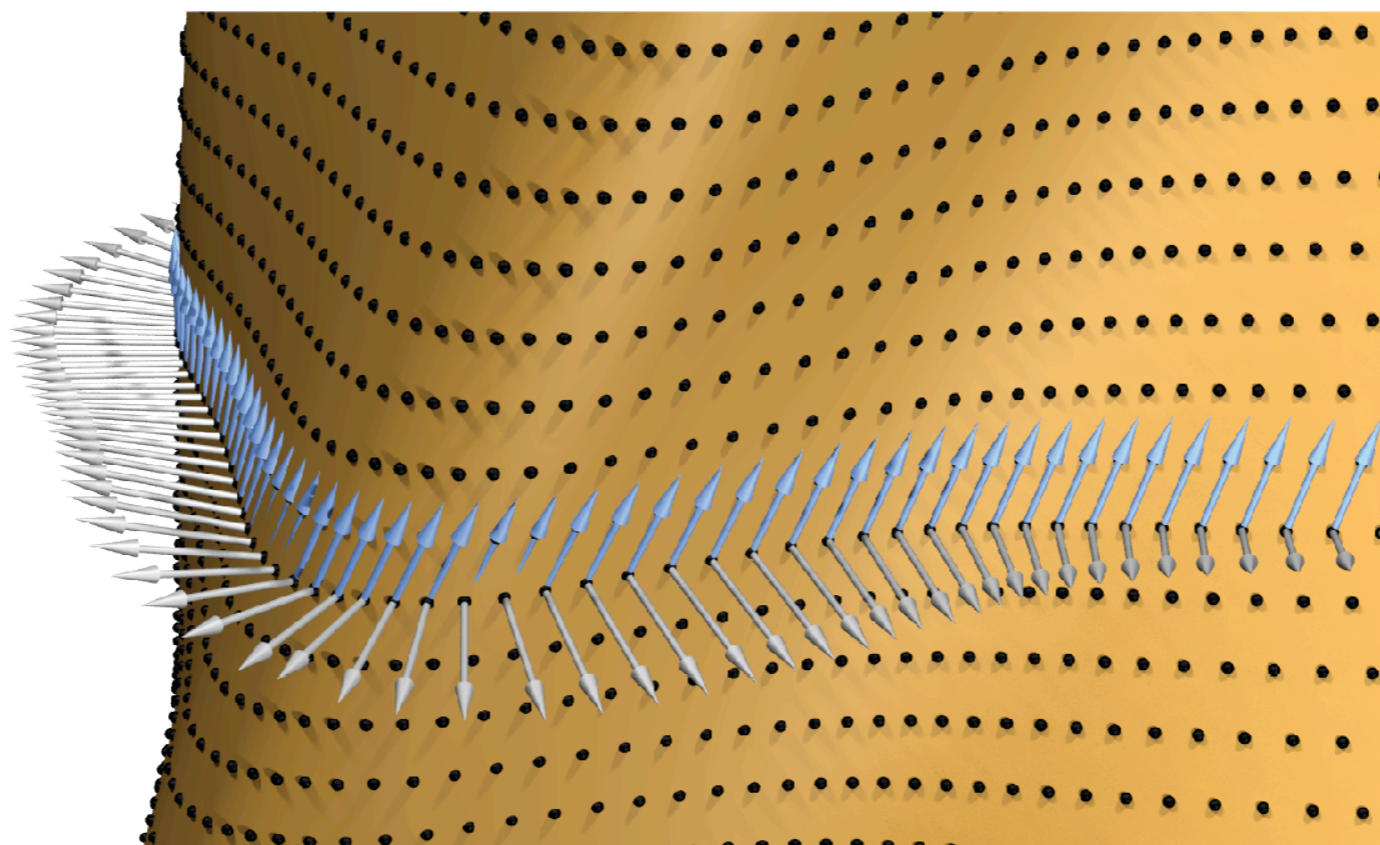
Spacetime Velocity Vectors



Tangential point movement \rightarrow velocity vectors orthogonal to surface normals

$$\widetilde{\alpha}_j = \operatorname{argmin} \sum_{i=1}^{|P^j|} d^2(\widetilde{\alpha}_j(\widetilde{\mathbf{p}}_i^j), S)$$

Spacetime Velocity Vectors



Tangential point movement \rightarrow velocity vectors orthogonal to surface normals

Final Steps

(rigid) velocity vectors \rightarrow $\tilde{\mathbf{v}}(\tilde{\mathbf{p}}_i^j) = (\mathbf{c}_j \times \mathbf{p}_i^j + \bar{\mathbf{c}}_j, 1)$

$$\min_{\mathbf{c}_j, \bar{\mathbf{c}}_j} \sum_{i=1}^{|P^j|} w_i^j \left[(\mathbf{c}_j \times \mathbf{p}_i^j + \bar{\mathbf{c}}_j, 1) \cdot \tilde{\mathbf{n}}_i^j \right]^2$$

Final Steps

(rigid) velocity vectors ! $\tilde{\mathbf{v}}(\tilde{\mathbf{p}}_i^j) = (\mathbf{c}_j \times \mathbf{p}_i^j + \bar{\mathbf{c}}_j, 1)$

$$\min_{\mathbf{c}_j, \bar{\mathbf{c}}_j} \sum_{i=1}^{|P^j|} w_i^j \left[(\mathbf{c}_j \times \mathbf{p}_i^j + \bar{\mathbf{c}}_j, 1) \cdot \tilde{\mathbf{n}}_i^j \right]^2$$

$$\mathbf{A}\mathbf{x} + \mathbf{b} = \mathbf{0}$$

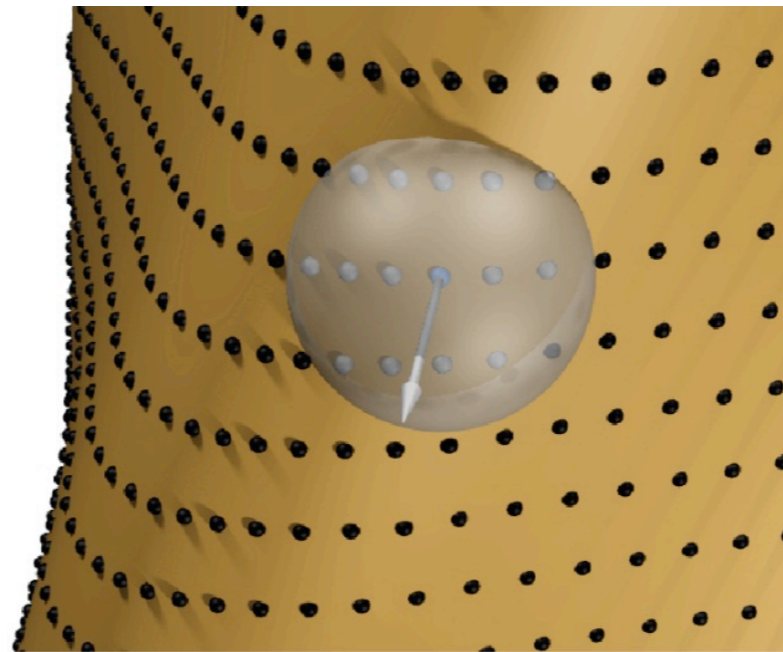
$$\mathbf{A} = \sum_{i=1}^{|P^j|} w_i^j \begin{bmatrix} \tilde{\mathbf{n}}_i^j \\ \mathbf{p}_i^j \times \tilde{\mathbf{n}}_i^j \end{bmatrix} \begin{bmatrix} \tilde{\mathbf{n}}_i^j{}^T & (\mathbf{p}_i^j \times \tilde{\mathbf{n}}_i^j)^T \end{bmatrix}$$

$$\mathbf{b} = \sum_{i=1}^{|P^j|} w_i^j n_i^j \begin{bmatrix} \tilde{\mathbf{n}}_i^j \\ \mathbf{p}_i^j \times \tilde{\mathbf{n}}_i^j \end{bmatrix} \quad \mathbf{x} = \begin{bmatrix} \bar{\mathbf{c}}_j \\ \mathbf{c}_j \end{bmatrix}$$

Registration Algorithm

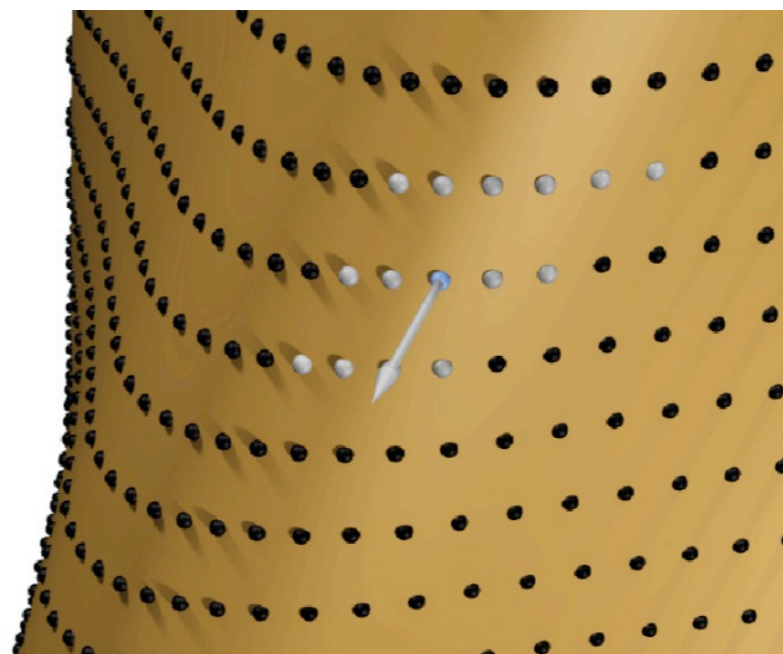
- 1. Compute time coordinate spacing (σ), and form space-time surface.**
- 2. Compute space time neighborhood using ANN, and locally estimate space-time surface normals.**
- 3. Solve linear system to estimate (c_j, \bar{c}_j).**
- 4. Convert velocity vectors to rotation matrix + translation vector using Plücker coordinates and quaternions.**

Normal Estimation: PCA Based



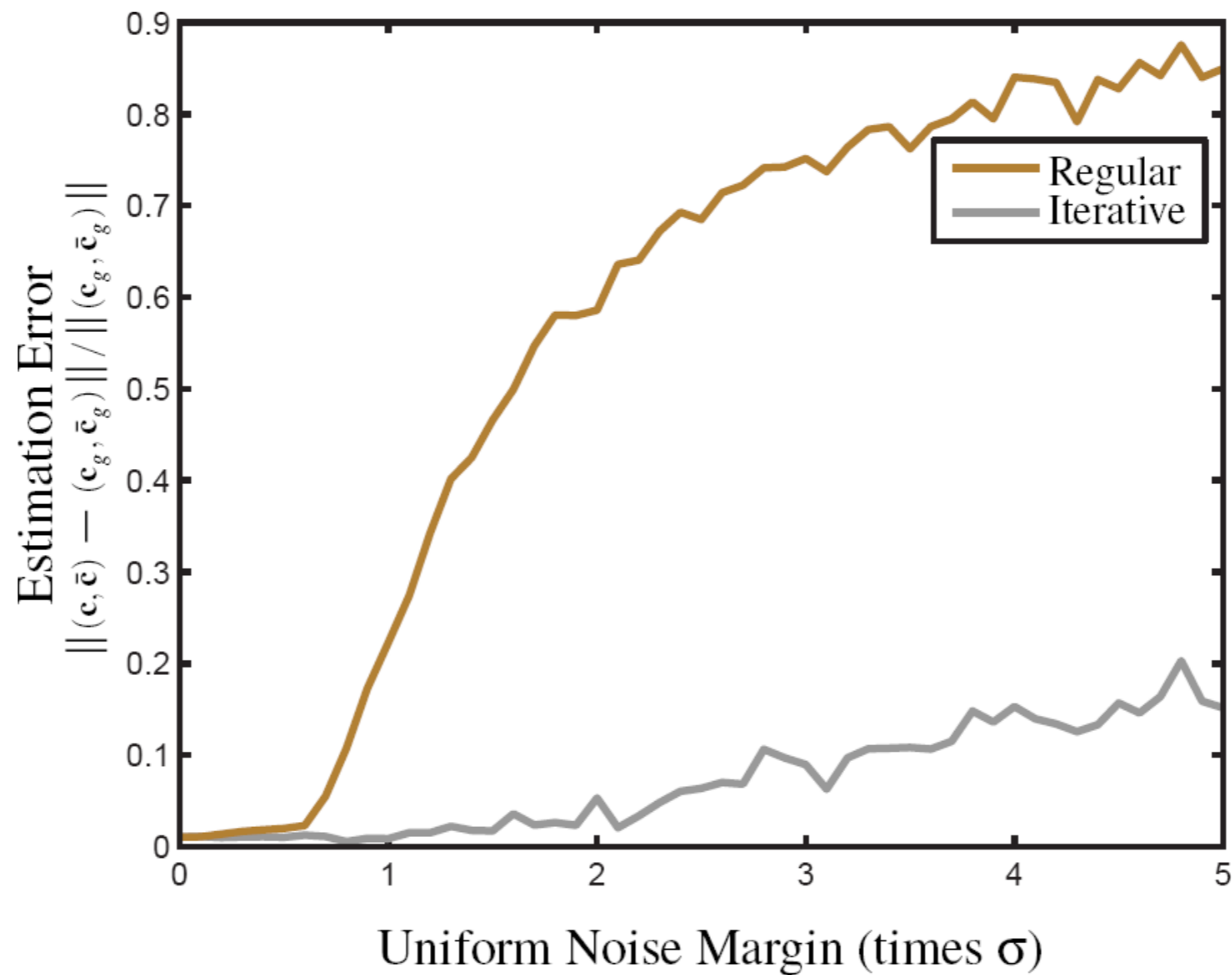
Plane fitting using PCA using chosen neighborhood points.

Normal Estimation: Iterative Refinement



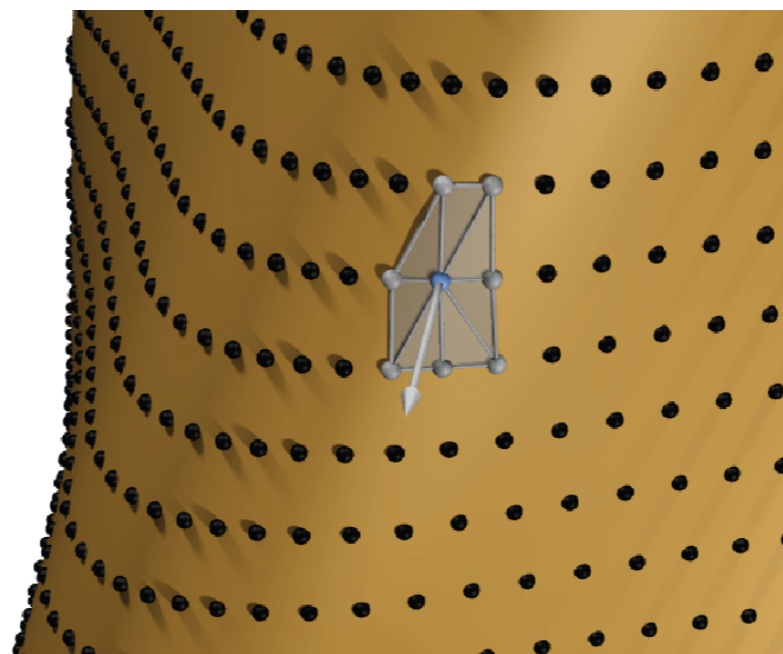
Update neighborhood with current velocity estimate.

Normal Refinement: Effect of Noise



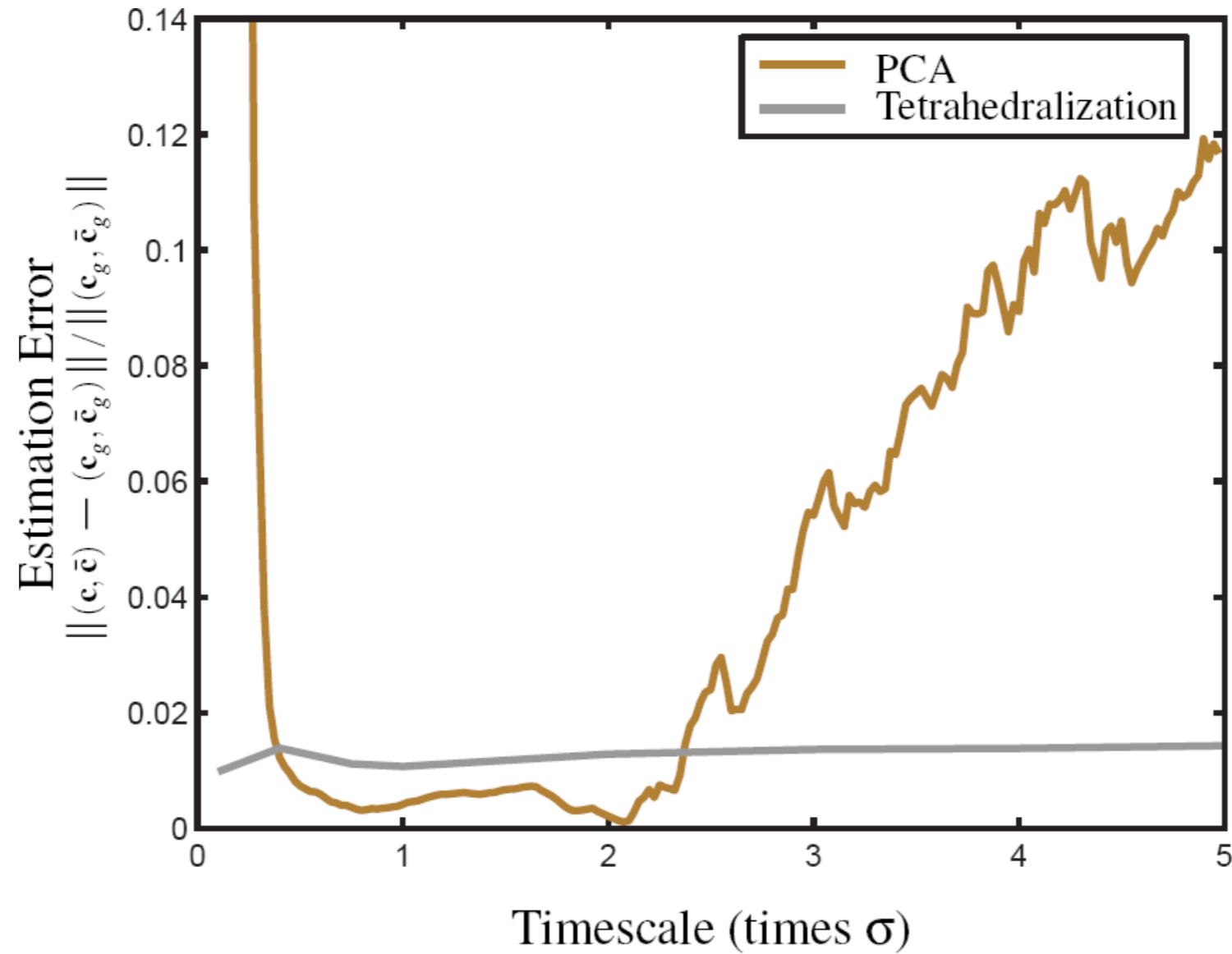
Stable, but more expensive.

Normal Estimation: Local Triangulation



Perform local surface triangulation (tetrahedralization).

Normal Estimation



Stable, but more expensive.

Comparison with ICP



ICP point-plane



Dynamic registration

Rigid: Bee Sequence (2,200 frames)

Bee

Input frames (Selection)

2200 pointclouds scanned at 17 Hz

transformations only for adjacent frames considered

no global error correction

no noise smoothing

Rigid: Coati Sequence (2,200 frames)

Coati

Input frames (Selection)

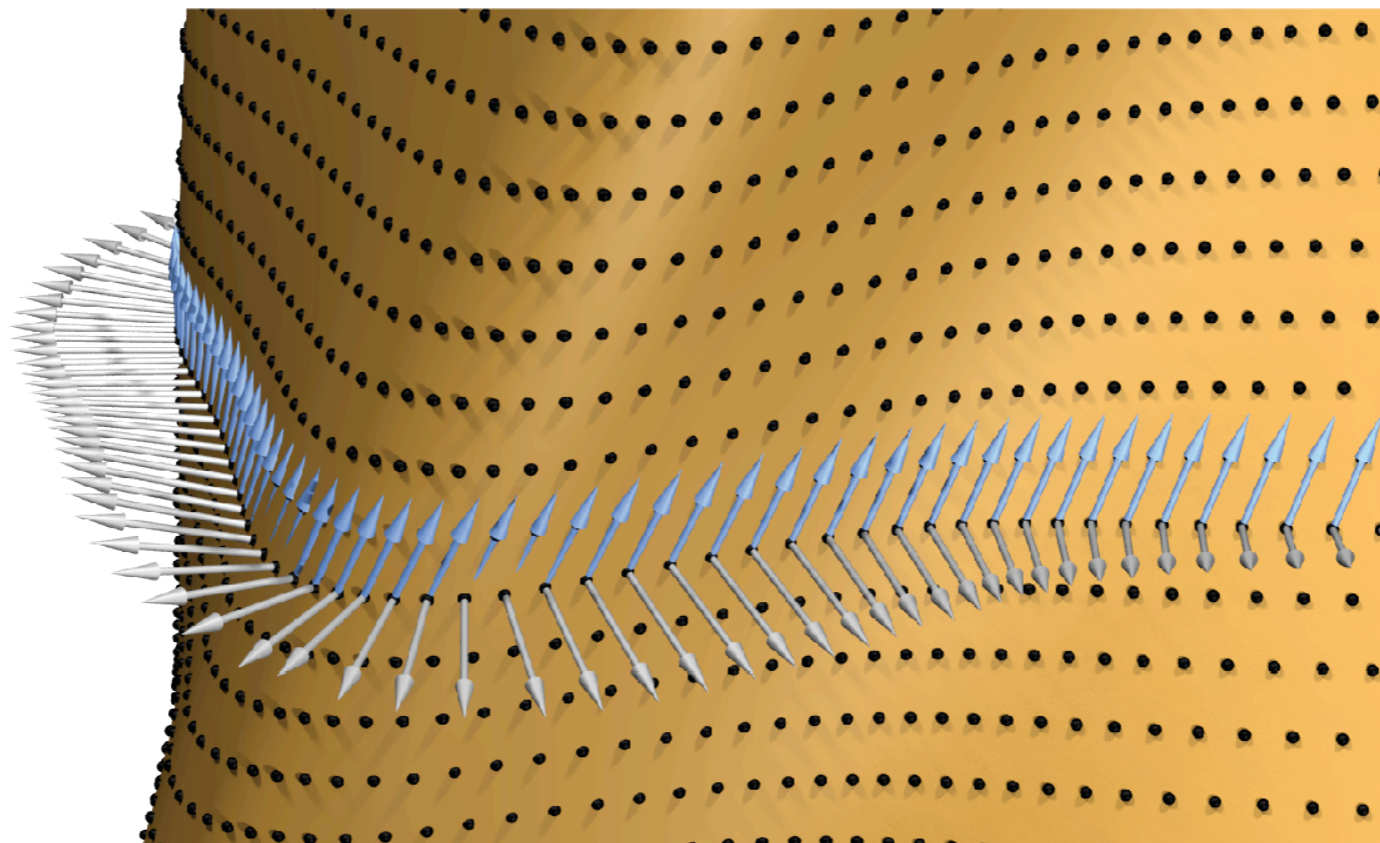
2200 pointclouds scanned at 17 Hz

transformations only for adjacent frames considered

no global error correction

no noise smoothing

Handling Large Number of Frames



Rigid/Deformable: Teapot Sequence (2,200 frames)

Teapot Input frames (Selection)

2200 pointclouds scanned at 17 Hz

transformations only for adjacent frames considered

no global error correction

no noise smoothing

Deformable Bodies

$$\min_{\mathbf{c}_j, \bar{\mathbf{c}}_j} \sum_{i=1}^{|P^j|} w_i^j \left[(\mathbf{c}_j \times \mathbf{p}_i^j + \bar{\mathbf{c}}_j, \mathbf{1}) \cdot \tilde{\mathbf{n}}_i^j \right]^2$$

Cluster points, and solve smaller systems.

Propagate solutions with regularization.

Deformable: Hand (100 frames)

Hand

Input frames & registered result

100 pointclouds scanned at 17 Hz

transformations only for adjacent frames considered

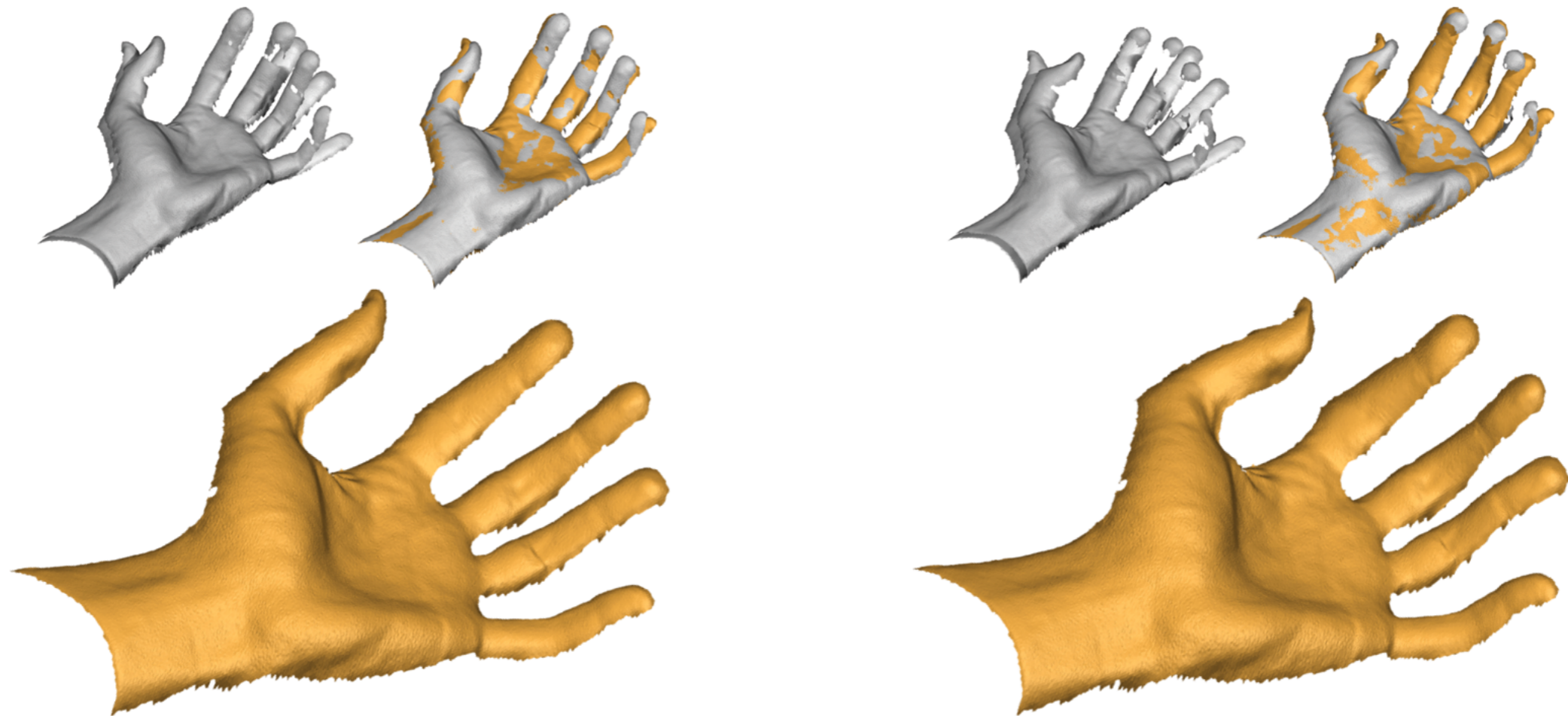
no global error correction

no noise smoothing

first frame is tracked

deformation due to severely missing data (e.g. ring finger)

Deformable: Hand (100 frames)



scan #1 : scan #50

scan #1 : scan #100

Deformation + scanner motion: Skeleton (100 frames)

Grasp

Input frames & registered result

100 **simulated** scan data sets

simultaneous object deformation and camera motion

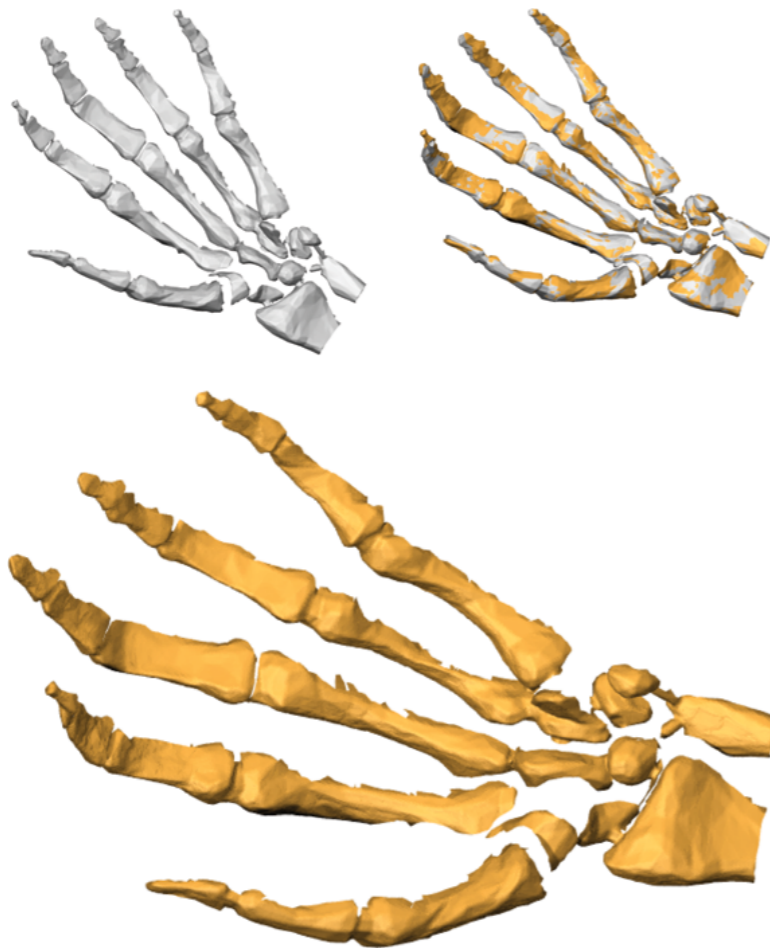
transformations only for adjacent frames considered

no global error correction, no noise smoothing

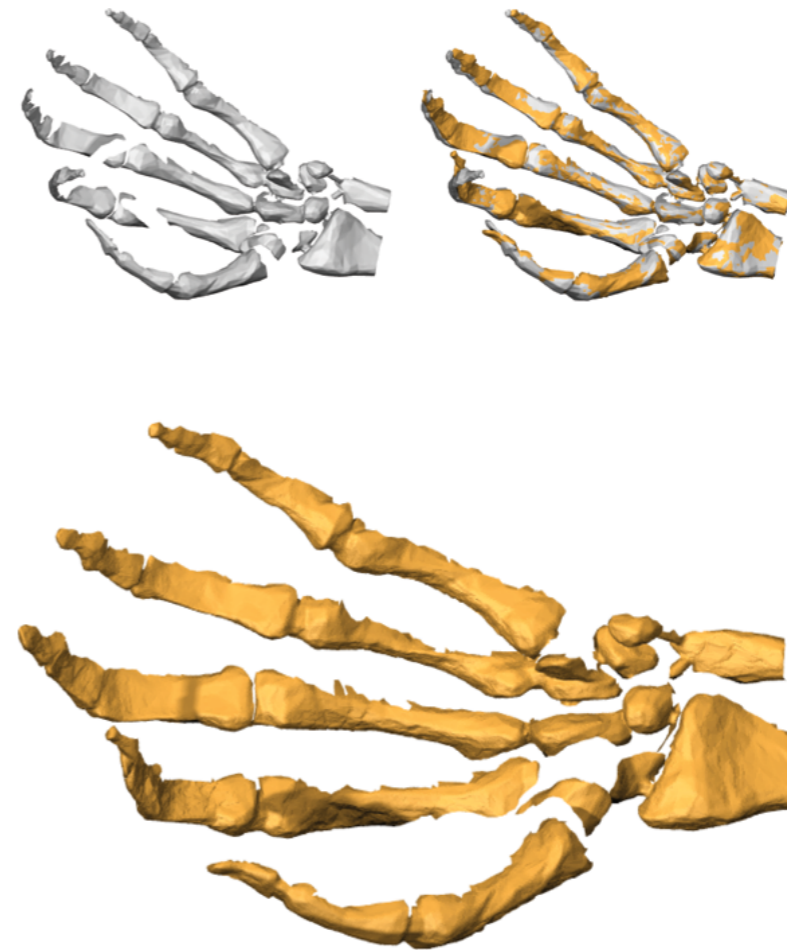
first frame is tracked

data completion (e.g. for middle finger)

Deformation + scanner motion: Skeleton (100 frames)

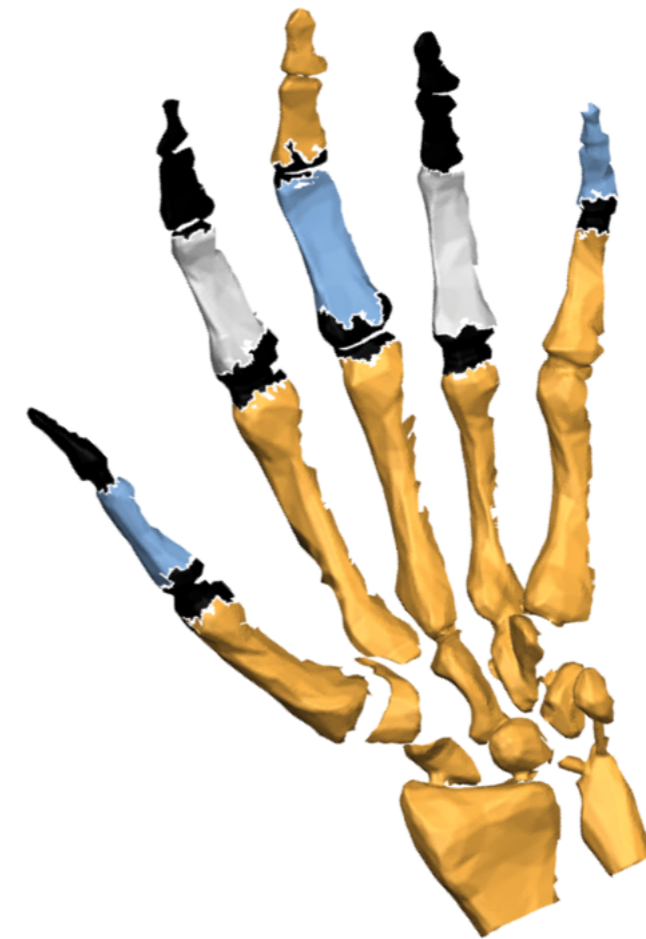
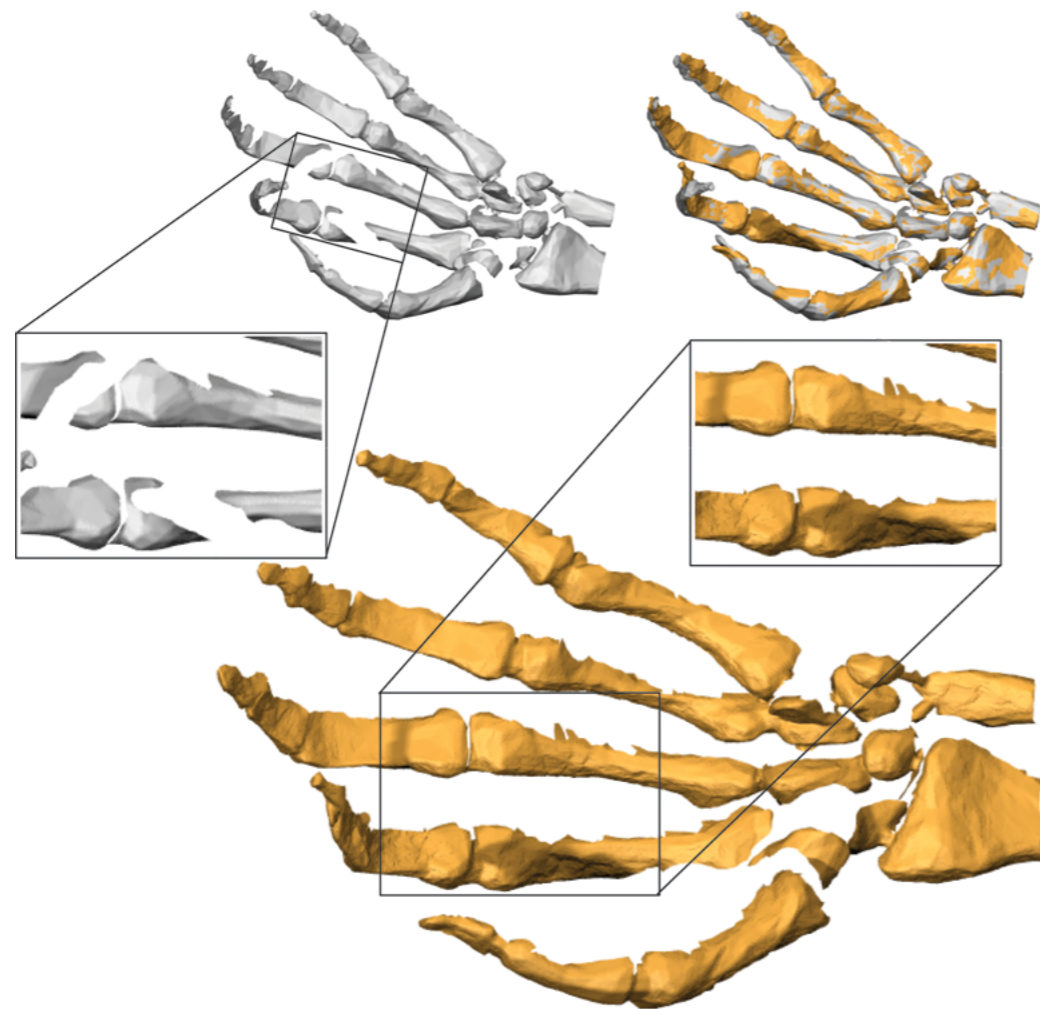


scan #1 : scan #50



scan #1 : scan #100

Deformation + scanner motion: Skeleton (100 frames)



rigid components

Performance (on 2.4GHz Athlon Dual Core, 2GB RAM)

Model	# scans	# points/scan (in 1000s)	Time (mins)
bunny (simulated)	314	33.8	13
bee	2,200	20.7	51
coati	2,200	28.1	71
teapot (rigid)	2,200	27.2	68
skeleton (simulated)	100	55.9	11
hand	100	40.1	17

Conclusion

Simple algorithm using kinematic properties of space-time surface.

Easy modification for deformable bodies.

Suitable for use with fast scanners.

Limitations

Need more scans, dense scans, ...

Sampling condition \rightarrow time and space



thank you

