

## Dániel Marx and Roohani Sharma

Summer 2023

10 points ——

Damer Marx and Rooman Sharma	Summer 2023
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cms.cispa.saarland/paramalg_23	
Total Points: 50	Due: Tuesday, <b>June 27</b> , 2023
own words. Please indicate the names of your collaboration	but you have to write down a solution on your own, using your orators for each exercise you solve. Further, cite all external sources You need to collect at least 50% of all points on exercise sheets to an .esmer@cispa.de).
— Exercise 1 —	4 + 4 + 2 points —
Let $G$ be an undirected graph, and let $s$ and	t be two vertices of $G$ .
(a) What is the maximum number of impor	extant $(s,t)$ -cuts of size exactly 1 in $G$ ?
(b) What is the maximum number of impor	etant $(s,t)$ -cuts of size exactly 2 in $G$ ?
(c) What is the maximum number of impor	rtant $(s,t)$ -cuts of size at most 2 in $G$ ?
Justify your answers.	
— Exercise 2 —	10 points
- ·	d $t$ be two vertices of $G$ . Is it true that the number of same as the number of important $(t,s)$ -cuts of size at
— Exercise 3 —	10 points
-	ECTED MULTIWAY CUT to DIRECTED MULTIWAY CUT given an instance $(G,T,k)$ of Undirected Multiway $(x,k)$ of Directed Multiway Cut.
— Exercise 4 —	10 points
Cut problem asks for a set $S$ of at most $k$ edge	ertices, and two integers $k$ and $\ell$ , the Short Multiway ges such that the graph $G-S$ contains no path of length show that the problem is FPT with combined parameters

In the MAX LEAF SUBTREE problem, given a graph G and integer k the goal is to find a sub-tree with at least k leaves. Show that this problem does not admit a polynomial kernel. You may use the fact that MAX LEAF SUBTREE is NP-complete.