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January 22, 2019

Tutorials for “Automated Reasoning WS18/19”  
Exercise sheet 12

**Exercise 12.1 (6.7):**

Use the FM method to decide whether the following conjunction of inequations is satisfiable:

$$x + y \geq 16 \quad (1)$$

$$4x + 7y \leq 28 \quad (2)$$

$$2x - 7y \leq 20 \quad (3)$$

$$2x - 3y \geq -9 \quad (4)$$

**Exercise 12.2 (6.6):**

Check via FM whether the following formulas are true/false

1.  $\forall x. \exists y. (2x + y > 7 \wedge x + y < 6)$

2.  $\exists x. \forall y. (2x - y > 7 \wedge 2x + y > 7)$

**Exercise\* 12.3 (6.9):**

Prove that unsatisfiability of a first-order  $\Sigma_{LA}$  formula over the free first-order logic semantics is undecidable.

It is not encouraged to prepare joint solutions, because we do not support joint exams.